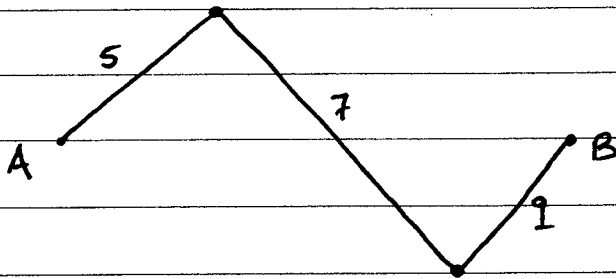


HOMEWORK #12

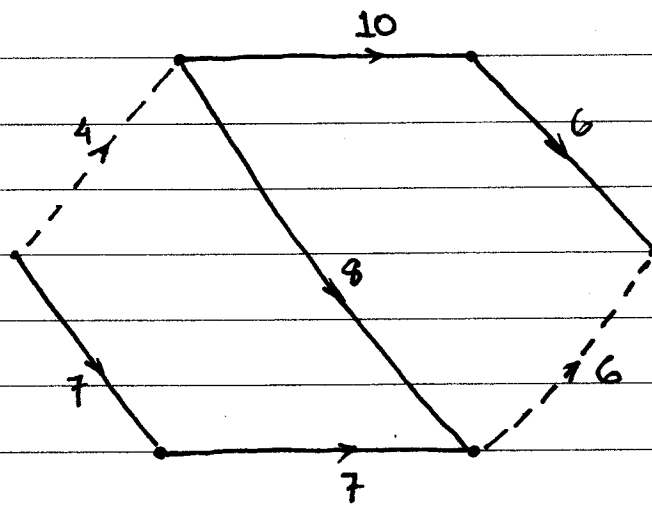
Problem 1:

Pg 270-271

#8:



#14:



The minimal cut is given by the dashed lines.

The maximal flow from A to B is $4 + 6 = 10$,

i.e.

the sum of the cut edge values.

Problem #2

Pg 279

#18)

If the k^{th} step of the algorithm takes 2^k seconds to execute, then to execute 40 steps we will require

$$\sum_{k=1}^{40} 2^k \text{ seconds} = 0.874 \times 10^{12} \text{ seconds}$$

However, this does not take into account the speed of the computer, i.e., 10^9 operations/second.

Therefore, had the question be framed as:

The k^{th} step takes 2^k operations to perform, then time required to perform 40 operations will be:

$$\frac{1}{10^9} \sum_{k=1}^{40} 2^k = 0.61 \text{ hours}$$

Pg-280

#26)

By Stirling's formula:

$$5! = \sqrt{10\pi} \left(\frac{5}{e}\right)^5 = 118.0192$$

Using series:

$$5! = \sqrt{10\pi} \left(\frac{5}{e}\right)^5 \left(1 + \frac{1}{12 \times 6} + \frac{1}{288 \times 6^2}\right) = 119.67$$

$$51 = 120$$

$$\% \text{ error} = \text{(i) for formula: } \frac{120 - 118.0192}{120} \times 100$$

$$= 1.65\% \quad \text{ANS}$$

$$\text{(ii) for series: } \frac{120 - 119.67}{120} \times 100$$

$$= 0.275\% \quad \text{Ans}$$

#28

By Stirling's Formula:

$$12! = \sqrt{24\pi} \left(\frac{12}{e} \right)^{12} = 475687486.4728$$

Using Series:

$$12! = \sqrt{24\pi} \left(\frac{12}{e} \right)^{12} \left(1 + \frac{1}{12 \times 13} + \frac{1}{288 \times 13^2} \right)$$

$$= 478746538.5616$$

$$12! = 479001600$$

% error

(i) for formula: 0.69%

(ii) for series: 0.053%

ANS

Problem #7

Pg 309

#10) $n=6$, $P(X=3)$ $P(X \leq 2)$

$$P(X \leq 2) = \binom{6}{0} \left(\frac{1}{2}\right)^6 + \binom{6}{1} \left(\frac{1}{2}\right) \left(\frac{1}{2}\right)^5 + \binom{6}{2} \left(\frac{1}{2}\right)^2 \left(\frac{1}{2}\right)^4$$

$$= \frac{11}{32} \text{ Ans}$$

#12) $n=8$, $P(X \leq 3)$

$$P(X \leq 3) = \binom{8}{0} \left(\frac{1}{2}\right)^8 + \binom{8}{1} \left(\frac{1}{2}\right) \left(\frac{1}{2}\right)^7 + \binom{8}{2} \left(\frac{1}{2}\right)^2 \left(\frac{1}{2}\right)^6 + \binom{8}{3} \left(\frac{1}{2}\right)^3 \left(\frac{1}{2}\right)^5$$

$$= \frac{1}{256} \times 93$$

$$= \frac{93}{256} \text{ Ans}$$

#16) $n=5$, $P(X=4)$

Let p correspond to the probability of 'x'

$$\text{Then } P(X=4) = \binom{5}{4} (0.3)^4 (0.7)$$

$$= 0.02835 \text{ Ans}$$

p. 309

26)

$P(40 \leq x \leq 60)$ out of 100

$$= P\left(\frac{40-50}{5} \leq z \leq \frac{60-50}{5}\right)$$

$$= P(-2 \leq z \leq 2)$$

(using Z scores)

could also be done w/
Pascal's triangle, but
would be very hard

$$= 0.95450 \text{ Ans}$$

$$\sum_{i=0}^{20} \binom{40+i}{100} / 2^{100}$$

When people appear to solve the Traveling Salesman problem they don't solve it in $O(2^n)$ time. Why not?

2^n time is a long time. When people 'solve' it, they are usually satisficing, or finding a good solution. Genetic algorithms & simulated annealing generally do not find the best answer, as well. They tend to find pretty good answers.

So, unless people ~~are~~ have some hidden talent, they will have to either take $O(\text{or } 2^n)$ time, or else just return a good answer.

Problem #3

Pg-275.

The solution has been taken from the book
'DISCRETE MATHEMATICAL STRUCTURES'
by Kolman, Busby, Ross, pg. 178.

178 Chapter 5 Functions

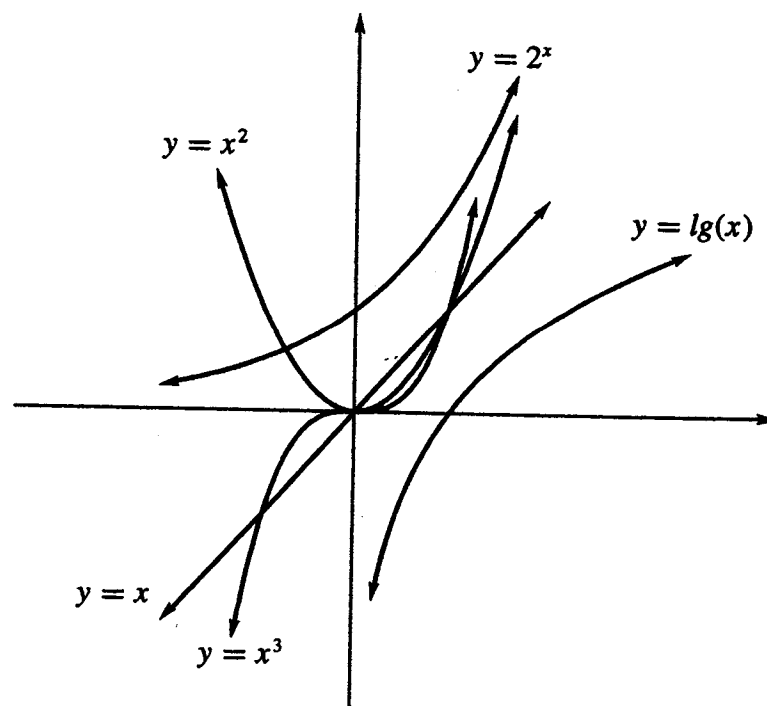


Figure 5.4